

Q1. Answer all of the following questions.

(a) [2 marks] Give a counterexample to the following statement.

"If  $a$  and  $b$  are integers with  $a - b \geq 0$  and  $b - a \geq 0$ , then  $a \neq b$ ."

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(b) [2 marks] If  $x \notin A \cup B$ . Which of the following is true,  $x \in A$  or  $x \notin A$ ? Justify your answer.

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Continue Q1 :

(c) [4 marks] Let  $K = \{1, \{\emptyset\}\}$ . Find  $\mathcal{P}(K)$  and  $|\mathcal{P}(\mathcal{P}(K))|$ .

$\mathcal{P}(K) = \{$  -----  
 $|\mathcal{P}(\mathcal{P}(K))| =$  -----

(d) [2 marks] For all sets  $A, B$ , and  $C$ , draw Venn Diagram such that  $A \subseteq C$ ,  $B \subseteq C$ , and  $A \cap B \neq \emptyset$ .

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Q2. [10 marks] For any integers  $a$  and  $b$ , if  $a^2 + b^2$  is divisible by 4, then either  $a$  is not odd or  $b$  is not odd.

A large rectangular box with a black border, containing 20 horizontal dashed lines for writing the answer.

Q3. Let  $U = \{n \in \mathbb{Z} \mid -3 \leq n \leq 3\}$ ,  $A_i = \{-i, i\}$ . Find the following:

(a) [2 marks]  $(A_1 \cup A_2) \cap \overline{A_3} =$

(b) [4 marks] Is  $\{A_1, A_2, A_3\}$  a partition of  $U$ ? Justify your answer.

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Q4. [10 marks] For all sets  $A$  and  $B$ , prove that  $(A - B) \cup (B - A) \cup (A \cap B) = A \cup B$ .

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